A dynamic theory of spatial externalities

Raouf Boucekkine¹, Giorgio Fabbri^{*2}, Salvatore Federico³, and Fausto Gozzi⁴

¹Aix-Marseille Sciences Economiques – École des Hautes Études en Sciences Sociales : UMR7316, Aix Marseille Université : UMR7316, Ecole Centrale de Marseille : UMR7316, Centre National de la Recherche Scientifique : UMR7316 – France

 $^2 {\rm GAEL}$ - CNRS – Univ. Grenoble Alpes, CNRS, INRA, Grenoble INP, GAEL, 38000 Grenoble, France - France

³Università of Siena – Università degli Studi di Siena Rettorato, Via Banchi di Sotto 55, 53100 Siena, Italie

⁴Libera Universita Internazionale degli Studi Sociali Guido Carli di Roma (Luiss Guido Carli) – Viale Pola, 12 - 00198 - Rome, Italy, Italie

Résumé

In this paper, we revisit the theory of spatial externalities. In particular, we depart in several respects from the important literature studying the fundamental pollution free riding problem uncovered in the associated empirical works. First, instead

of assuming ad hoc pollution diffusion schemes across space, we consider a realistic spatiotemporal law of motion for air and water pollution (diffusion and advection). Second, we tackle spatiotemporal non-cooperative (and cooperative) differential games. Precisely, we consider a circle partitioned into several states where a local authority decides autonomously about its investment, production and depollution strategies over time knowing that investment/production generates pollution, and pollution is transboundary. The time horizon is infinite. Third, we allow for a rich set of geographic heterogeneities across

states while the literature assumes identical states. We solve analytically the induced noncooperative differential game under decentralization and fully characterize the resulting longterm spatial distributions. We further provide with full exploration of the free riding problem, reflected in the so-called border effects. In particular, net pollution flows diffuse at an increasing rate as we approach the borders, with strong asymmetries under advection, and structural breaks show up at the borders. We also build a formal case in which a larger number of states goes with the exacerbation of pollution externalities.

Finally, we explore how geographic discrepancies affect the shape of the border effects.

Mots-Clés: Spatial externalities, environmental federalism, transboundary pollution, differential games in continuous time and space, infinite dimensional optimal control problems

*Intervenant